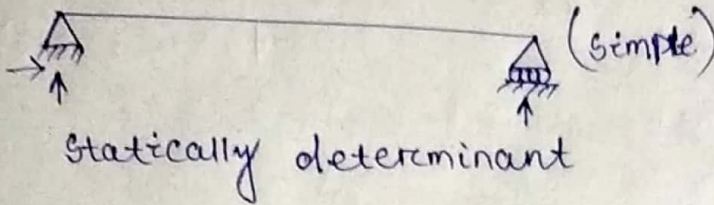
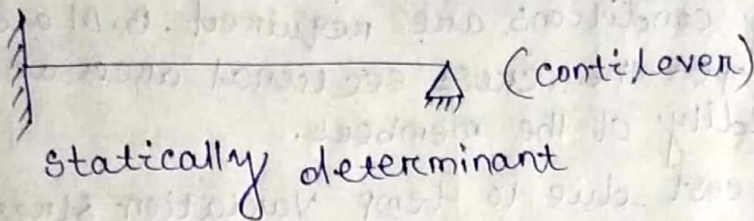


No. of equilibrium equation = no. of reaction force

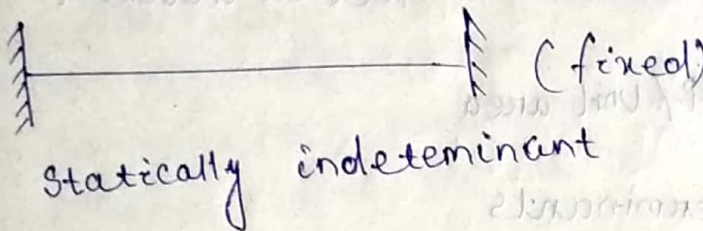
(1)



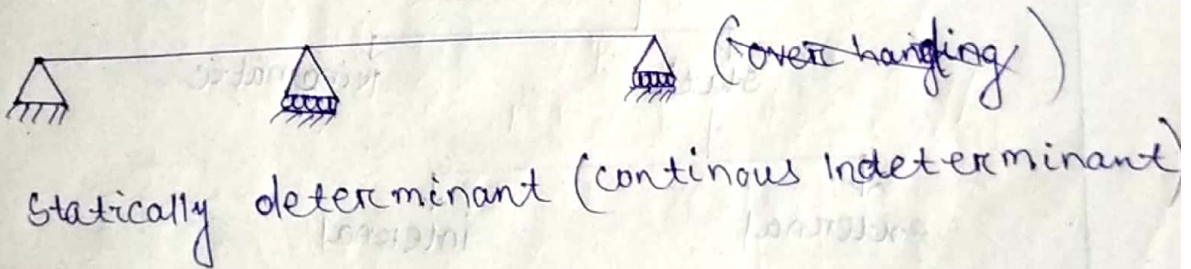
(2)



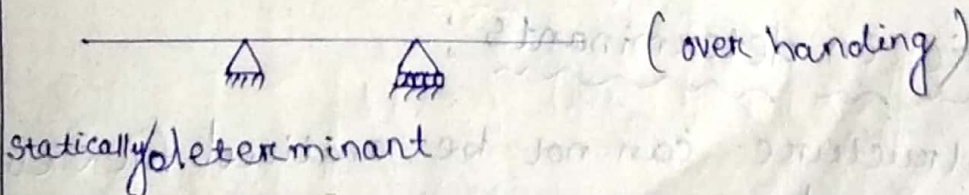
(3)



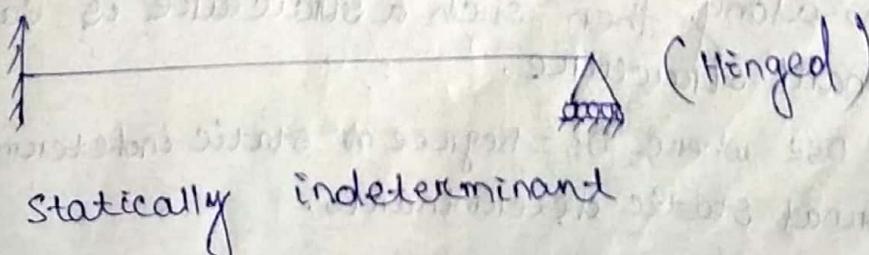
(4)



(5)



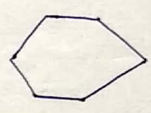
(6)



Statically determinate structure: conditions of equilibrium are sufficient to analyze the structure. B.M. and S.F. is independent of the cross-sectional area of the component and flexural rigidity of member. No stress are cast due to temperature change and due to load of.

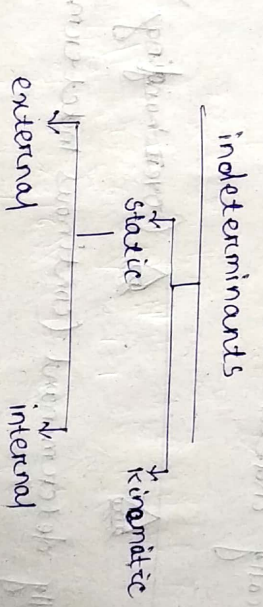
$$I = \frac{bh^3}{36}$$

feet on differential set element.



→ Statically indeterminate structure: Additional compatibility conditions are required. B.M and S.F are depends on the cross sectional area and flexural rigidity of the members. Stresses are cast due to temp variation stress are cast due to load of feet on differential settlement.

$$\text{Stress} = P / \text{unit area}$$



Static indeterminants:

A structure can not be analysed for external and internal reactions using static equilibrium conditions along then a structure is called indeterminate structure.

- ① $D_s = D_{se} + D_{si}$ where D_s = Degree of static indeterminants
- D_{se} = external static determinants.
- D_{si} = internal static indeterminants.

External static indeterminants:-

It is related with the support system of the structure and it is equal to no. of external reaction components in addition to no. of static reaction.

no. of reaction.
 $(D_{se} = R_e - 3 \rightarrow \text{no. of equilibrium equation}) \quad 2D$

total external reaction
 $(D_{se} = R_e - 6 - 3D)$

$\therefore R_e = \text{total external reaction.}$



Internal static Indeterminants:-

It is reinforced to the Geometric stability of the structure. It is after knowing the external reactions it is not possible to determine all internal forces or internal reactions using static equilibrium equation. along then the structure is set to be internally indeterminate.

(ii) for geometric stability, sufficient no. of members are required to prevent the same of body.

$D_{si} = 3C - R_r$

$C = \text{no. of closed circle.}$

$R_r = \text{released reaction}$

Ex:-

$6 - 5 = 1$
 $3 \times 2 - R_r = 1$
 $R_r = \sum (m_j - 1)$
 $= 6 - 1$
 $= 5$

$\rightarrow \text{No. of member.}$

$SI = (\alpha m + R_r) - (\beta j + \gamma)$

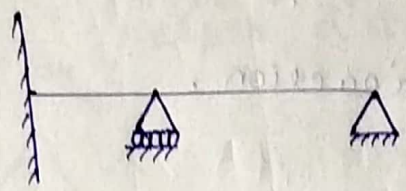
$M \rightarrow$ no. of member

$r \rightarrow$ no. of reaction

$\beta \rightarrow$ no. of equilibrium equation (3)

$j \rightarrow$ no. of joints

$\gamma \rightarrow$ no. of released



Formula

$$SI = (3 \times 2 * 6) - (3 \times 3 + 0)$$

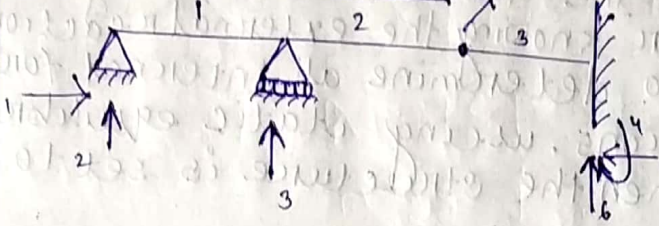
$$= 12 - 9 = 3$$

$$m = 2 \quad \alpha = 3$$

$$r = 6 \quad j = 3$$

$$\beta = 3$$

Beam: S.F, A.F, moment



Internal hinged

$$SI = (\alpha m + r) - (\beta j + \gamma)$$

~~Beam~~ S.F, A.F, moment

$$\alpha = 3 \quad \beta = 3$$

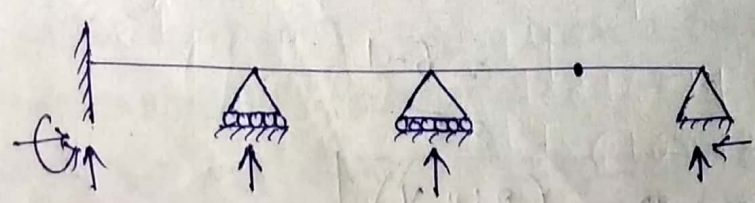
$$m = 3 \quad j = 4$$

$$r = 6 \quad \gamma = 2 - 1 = 1$$

$$SI = (3 \times 3 + 6) - (15 - 13)$$

$$= 2$$

S.F, A.F, and moment



$$\alpha = 3 \quad \beta = 3$$

$$m = 4 \quad j = 5$$

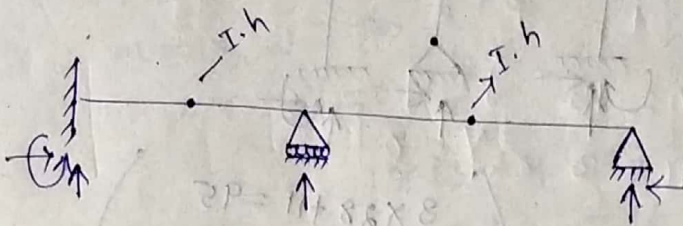
$$r = 7 \quad \gamma = 1$$

$$3 \times 4 + 7 = 19$$

$$3 \times 5 + 1 = 16$$

$$SI = 19 - 16$$

$$= 3$$



$$\alpha = 3 \quad \beta = 3$$

$$m = 4 \quad j = 5$$

$$r = 6 \quad \gamma = 2$$

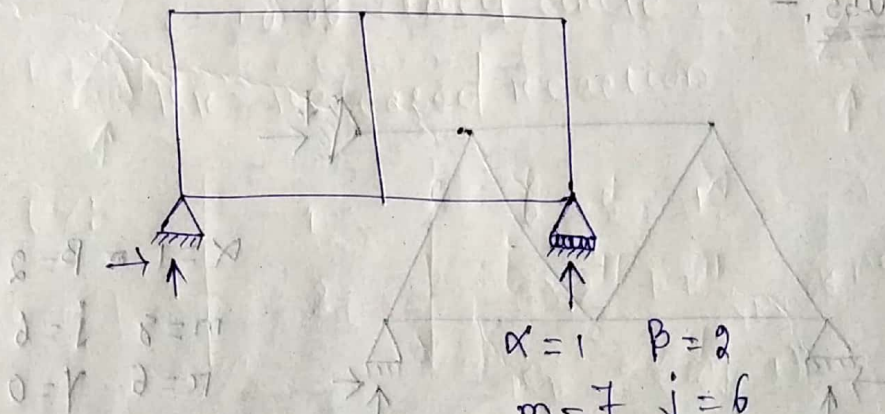
$$3 \times 4 + 6 = 18$$

$$3 \times 5 + 2 = 17$$

$$SI = 18 - 17$$

$$= 1$$

Trusses :-



$$\alpha = 1 \quad \beta = 2$$

$$m = 7 \quad j = 6$$

$$r = 3 \quad \gamma = 0$$

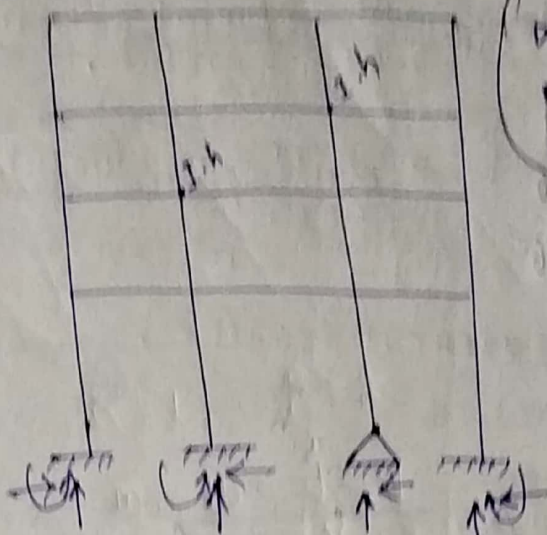
$$SI = 1 \times 7 + 3 = 10$$

$$2 \times 6 + 0 = 12$$

$$SI = 10 - 12$$

$$= -2$$

Frame :-



$$\left(\begin{array}{ll} \alpha = 3 & \beta = 3 \\ m = 28 & j = 20 \\ r = 11 & \gamma = 0 \end{array} \right)$$

$$\left(\begin{array}{l} 3 \times 28 + 11 = 95 \\ 3 \times 20 + 0 = 60 \\ SI = 95 - 60 = 35 \end{array} \right)$$

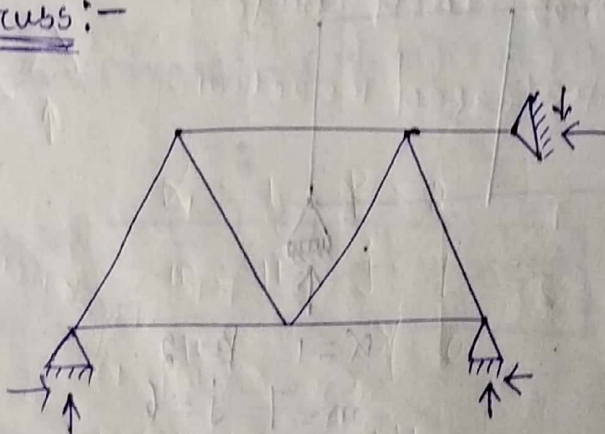
$$\begin{array}{ll} \alpha = 3 & \beta = 3 \\ m = 28 & j = 20 \\ r = 11 & \gamma = 6 \end{array}$$

$$3 \times 28 + 11 = 95$$

$$3 \times 20 + 6 = 66$$

$$SI = 95 - 66 = 29$$

Trauss :-



$$\begin{array}{ll} \alpha = 1 & \beta = 2 \\ m = 8 & j = 6 \\ r = 6 & \gamma = 0 \end{array}$$

$$1 \times 8 + 6 = 14$$

$$2 \times 6 + 0 = 12$$

$$SI = 14 - 12 = 2$$

$$II - 6 - 3D$$

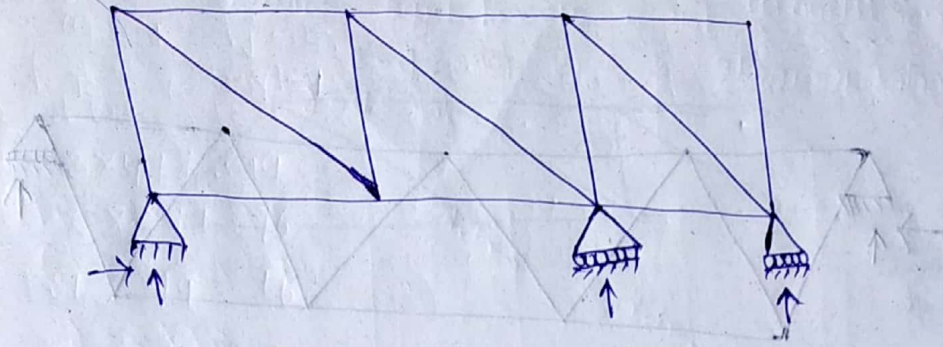
$$II - 8 - 2D \quad EI = r - 3$$

$$II = 27$$

$$= 8$$

$$SI = 35 - 6 = 29$$

1



$$\alpha = 1 \quad \beta = 2$$

$$m = 13 \quad j = 8$$

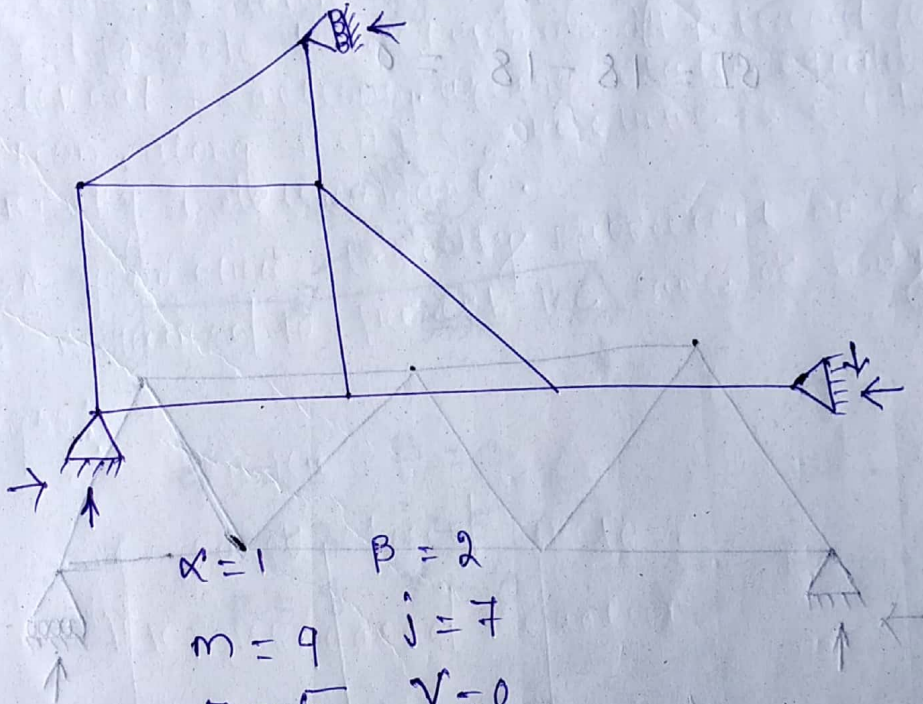
$$r = 4 \quad \gamma = 0$$

$$1 \times 13 + 4 = 17$$

$$2 \times 8 + 0 = 16$$

$$SI = 17 - 16 = 1$$

2



$$\alpha = 1 \quad \beta = 2$$

$$m = 9 \quad j = 7$$

$$r = 5 \quad \gamma = 0$$

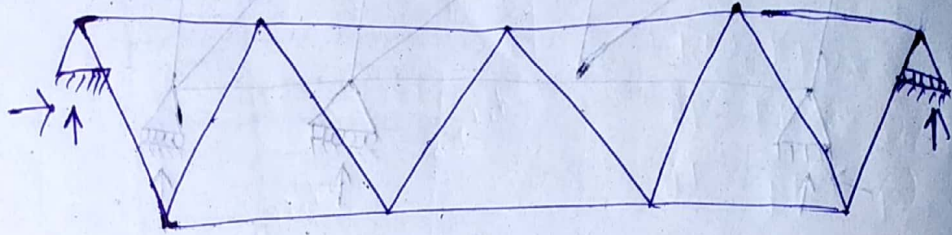
$$1 \times 9 + 5 = 14$$

$$2 \times 7 + 0 = 14$$

$$SI = 14 - 14$$

$$= 0$$

3



$$\alpha = 1 \quad \beta = 2$$

$$m = 15 \quad j = 9$$

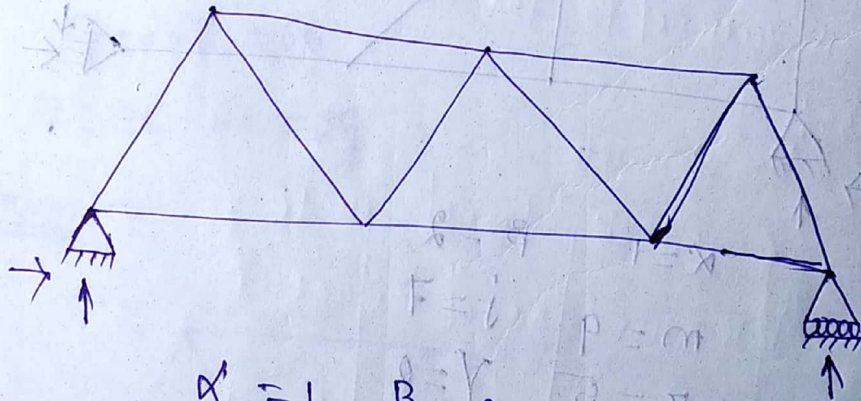
$$r = 3 \quad Y = 0$$

$$1 \times 15 + 3 = 18$$

$$2 \times 9 + 0 = 18$$

$$SI = 18 - 18 = 0$$

4



$$\alpha = 1 \quad \beta = 2$$

$$m = 11 \quad j = 7$$

$$r = 3 \quad Y = 0$$

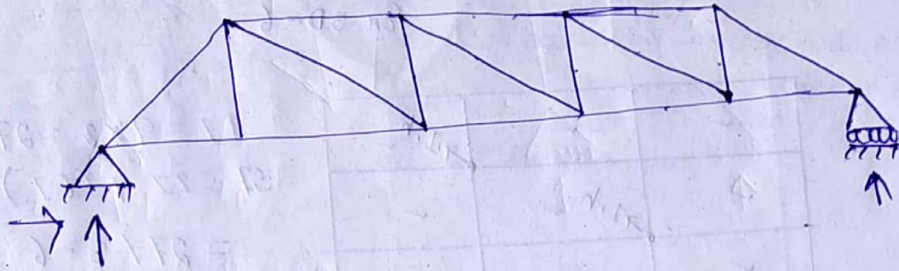
$$1 \times 11 + 3 = 14$$

$$2 \times 7 + 0 = 14$$

$$SI = 14 - 14$$

$$= 0$$

5



$$\alpha = 1 \quad \beta = 2$$

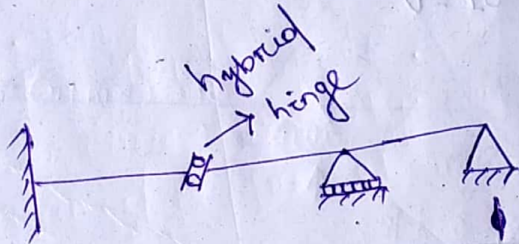
$$m = 17 \quad j = 10$$

$$r = 3 \quad \gamma = 0$$

$$1 \times 17 + 3 = 20$$

$$2 \times 10 + 0 = 20$$

$$SI = 20 - 20 = 0$$



$$\alpha = 3 \quad \beta = 3$$

$$m = 3 \quad j = 5$$

$$r = 8 \quad \gamma = 0$$

$$3 \times 3 + 8 = 17$$

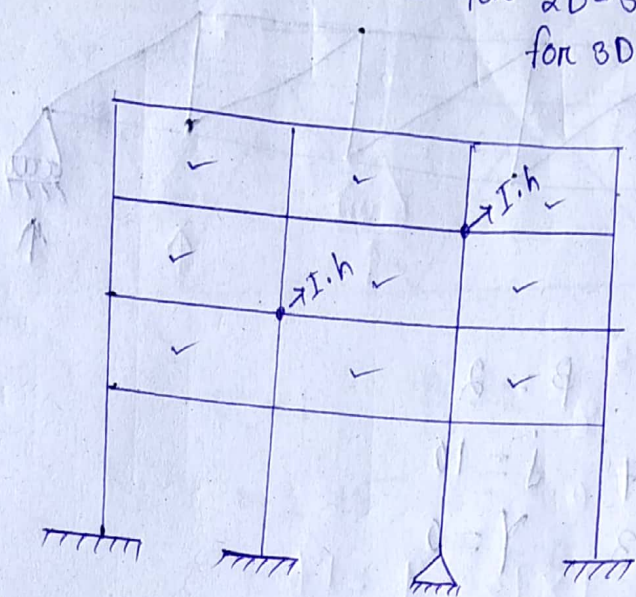
$$3 \times 5 + 0 = 15$$

$$SI = 17 - 15 = 2$$

SI = static Indeterminate
 KI = Kynamatic Indeterminate

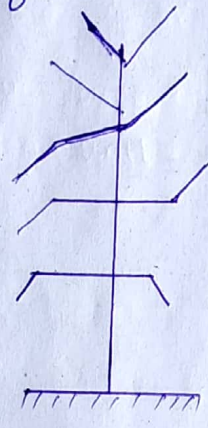
$$SI = (\alpha m + r) - (\beta j + \gamma)$$

Condition (1) for a closed type structure the internal Indeterminate () is for 2D-3
for 3D-6

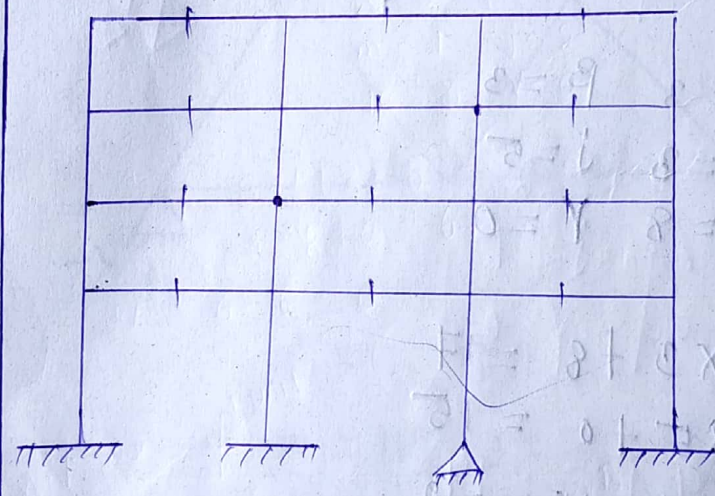


$$\begin{aligned}
 II &= 9 \times 3 = 27 \\
 SI &= II + (EI) \\
 &= 27 + 8 - 6 \\
 &= 29
 \end{aligned}$$

for a cantilever three types structure the $SI = 0$



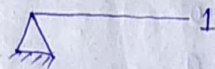
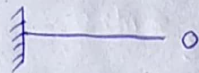
$$SI = 0$$



$$12 \times 3 = 36 - 7$$

SI = 29

KI - Kinematic Indeterminate (degree of freedom)

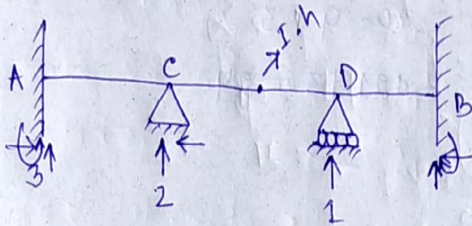


formula

$$KI = a_j - b + \gamma$$

a_j → No. of joint
 b → No. of reaction
 γ → No. of release
 No. degree of freedom available at 'c' joint.

$a = 3 (A_x, A_y, \theta_{xy})$



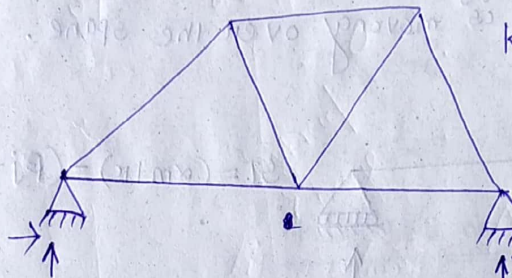
$j = 5 \quad \gamma = 1$

$b = 9$

$KI = 15 - 9 + 1$

$= 7$

Ex:-



$KI = a_j - b + \gamma$

$a = 2$

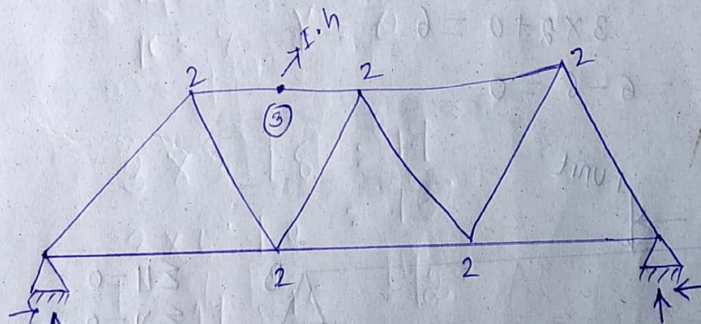
$2 \times 5 - 4 + 0$

$= 10 - 4$

$= 6$

Frame $a=3$

Ex:-



$a = 2$

$j = 8$

$b = 4$

$\gamma = 1$

$2 \times 8 - 4 + 1$

$= 16 - 5$

$= 11$

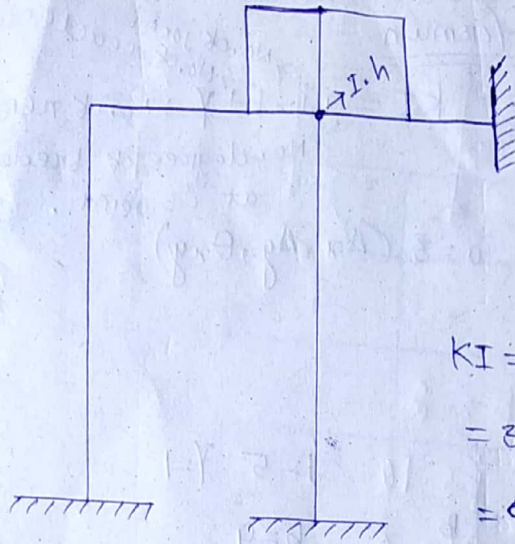
$= (2 \times 8) - (4 + 1)$

$= 16 - 5$

$= 12 + 1$

$= 13$

EX:-



$$a=3$$

$$j=10$$

$$b=9$$

$$\gamma=4-1=3$$

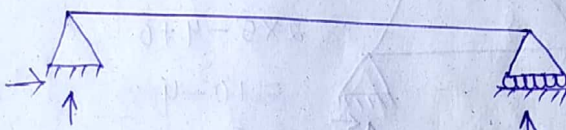
$$KI = 3 \times 10 - 9 + 3$$

$$= 30 - 9 + 3$$

$$= 21 + 3 = 24$$

ILD:- Influence line diagram.

→ is the graphical representation of various function (shear force, bending moment - axial force etc) when a unit load is moving over the span.



$$SI = (\alpha m + \pi) - (\beta j - \gamma)$$

$$\alpha=3 \quad \beta=3$$

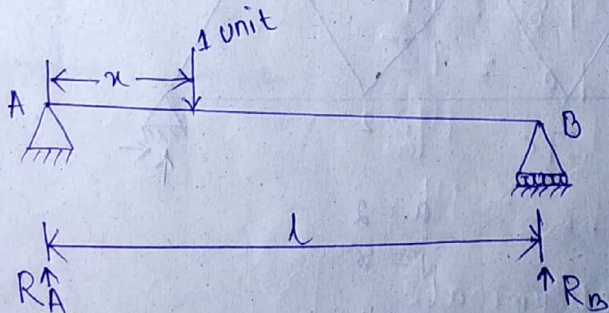
$$m=1 \quad j=2$$

$$\pi=3 \quad \gamma=0$$

$$3 \times 1 + 3 = 6$$

$$3 \times 2 + 0 = 6$$

$$SI = 6 - 6 = 0$$



$$\sum H = 0$$

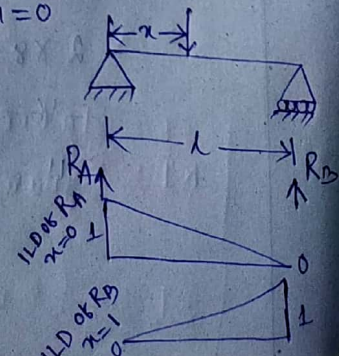
$$\sum V = 0$$

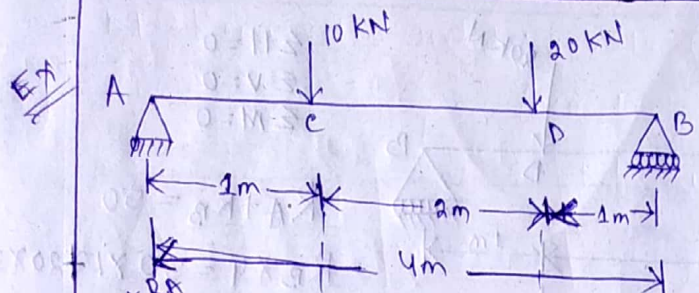
$$\sum M = 0$$

$$R_A + R_B = 1 \quad \text{--- (1)} \Rightarrow R_A = 1 - R_B$$

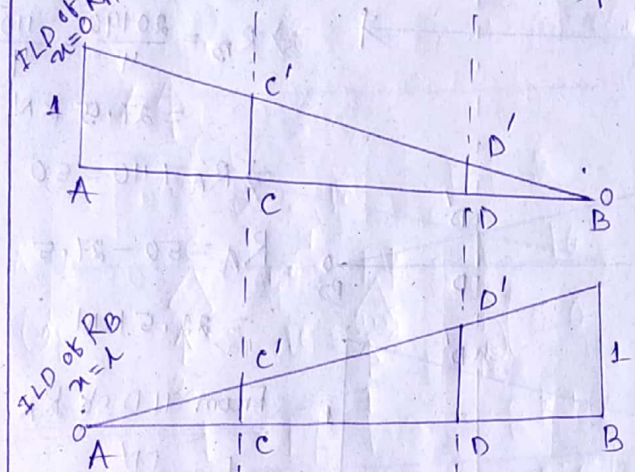
$$R_B \times l = x \Rightarrow R_B = x/l$$

value of $R_B = x/l$ --- (2) value of $R_A = 1 - x/l$

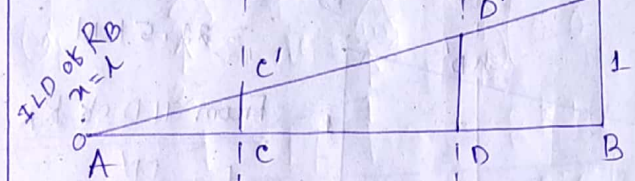




$$\begin{aligned} \sum H &= 0 \\ \sum V &= 0 \\ \sum M &= 0 \end{aligned}$$



$$\begin{aligned} R_A + R_B &= 30 \\ R_B \times 4 &= 10 \times 1 + 20 \times 3 \\ \Rightarrow R_B &= \frac{70}{4} = 17.5 \text{ KN} \\ \Rightarrow R_A &= 30 - 17.5 \\ R_A &= 12.5 \text{ KN} \end{aligned}$$



From ILD of R_A

$$\frac{1}{L} = \frac{DD'}{L}$$

$$\Rightarrow DD' = \frac{1}{L} \quad \text{--- (1)}$$

$$= \frac{1}{L} = \frac{CC'}{3}$$

$$\Rightarrow CC' = 3/L \quad \text{--- (2)}$$

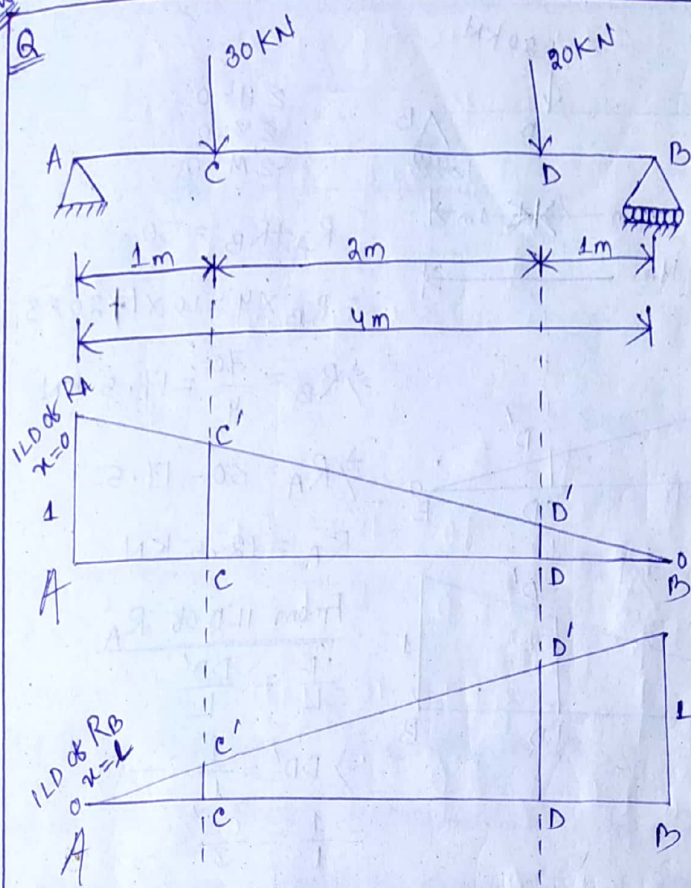
$$\begin{aligned} R_A &= 10 \times \frac{5}{4} + 20 \times \frac{1}{4} \\ &= 5 + 5 = 10 \text{ KN} \end{aligned}$$

From ILD of R_B

$$\begin{aligned} \Rightarrow \frac{1}{4} &= \frac{CC'}{1} \\ \Rightarrow CC' &= \frac{1}{4} \quad \text{--- (1)} \\ \Rightarrow \frac{1}{4} &= \frac{DD'}{3} \\ \Rightarrow DD' &= \frac{3}{4} \end{aligned}$$

$$\begin{aligned} R_B &= 20 \times \frac{3}{4} + 10 \times \frac{1}{4} \\ &= 17.5 \text{ KN} \end{aligned}$$

H.W



$$\begin{aligned} \sum H &= 0 \\ \sum V &= 0 \\ \sum M &= 0 \end{aligned}$$

$$\begin{aligned} R_A + R_B &= 50 \\ R_B \times 4 &= 30 \times 1 + 20 \times 3 \\ \Rightarrow R_B &= \frac{20 + 60}{4} = \frac{80}{4} \\ &= 20 \text{ kN} \end{aligned}$$

$$\begin{aligned} \Rightarrow R_A + 20 &= 50 \\ R_A &= 50 - 20 \\ &= 30 \text{ kN} \end{aligned}$$

From ILD of R_A

$$\frac{1}{L} = \frac{DD'}{L}$$

$$\Rightarrow DD' = \frac{1}{L} \quad \text{--- (1)}$$

$$= \frac{1}{L} = \frac{CC'}{3}$$

$$\Rightarrow CC' = \frac{3}{L} \quad \text{--- (2)}$$

$$\begin{aligned} R_A &= 20 \times \frac{3}{4} + 30 \times \frac{1}{4} \\ &= 22.5 \text{ kN} \end{aligned}$$

From ILD of R_B

$$\Rightarrow \frac{1}{4} = \frac{CC'}{1}$$

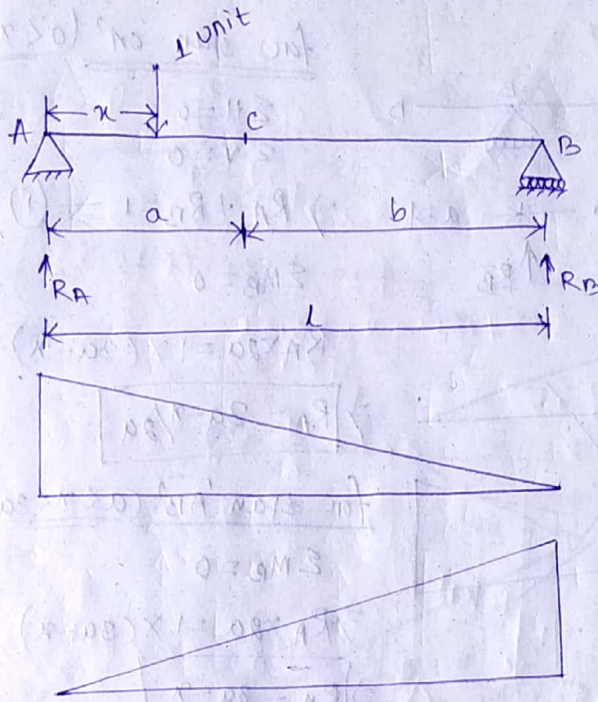
$$\Rightarrow CC' = \frac{1}{4} \quad \text{--- (1)}$$

$$\Rightarrow \frac{1}{4} = \frac{DD'}{3}$$

$$\Rightarrow DD' = \frac{3}{4}$$

$$\begin{aligned} R_B &= 20 \times \frac{1}{4} + 30 \times \frac{3}{4} \\ &= 27.5 \text{ kN} \end{aligned}$$

Ex:

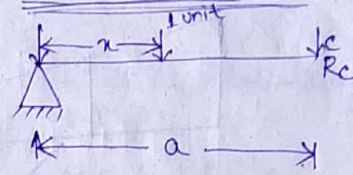


$$L = a + b$$

$$R_A = \frac{L-x}{L}$$

$$R_B = x/L$$

For the span 'Ac' ($0 < x < a$)



$$\Rightarrow R_A = 1 + R_c$$

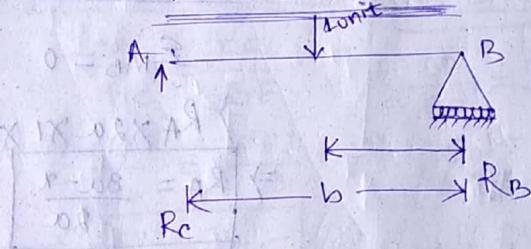
$$\Rightarrow R_c = R_A - 1$$

$$= \frac{L-x}{L} - 1$$

$$= \frac{L-x-L}{L}$$

$$R_c = -x/L$$

For the span 'CB' ($a < x < L$ or $(a+b)$)



$$R_c + R_B = 1$$

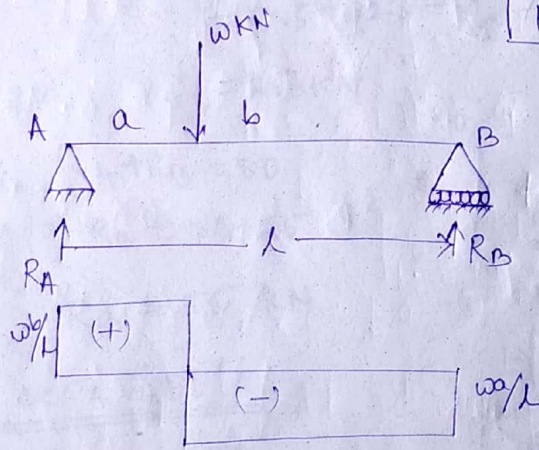
$$R_c = 1 - R_B$$

$$= 1 - x/L$$

$$R_c = \frac{L-x}{L}$$

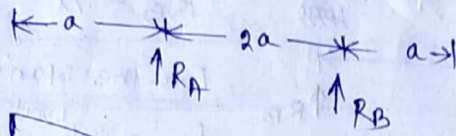
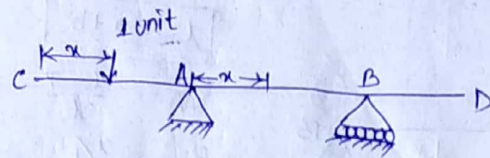
Ans

Ex



($0 < x < a$)

Q



for span 'CA' ($0 < x < a$)

$$\sum H = 0$$

$$\sum V = 0$$

$$\Rightarrow R_A + R_B = 1 \quad \text{--- (1)}$$

$$\sum M_B = 0$$

$$R_A \times 2a = 1 \times (3a - x)$$

$$\Rightarrow R_A = \frac{3a - x}{2a}$$

for span 'AB' ($a < x < 3a$)

$$\sum M_B = 0$$

$$\Rightarrow R_A \times 2a = 1 \times (3a - x)$$

$$\Rightarrow R_A = \frac{3a - x}{2a}$$

for span 'BD' ($3a < x < 4a$)

$$\sum M_B = 0$$

$$\Rightarrow R_A \times 2a \times 1 \times (x - 3a) = 0$$

$$\Rightarrow R_A = \frac{3a - x}{2a}$$

$$\Rightarrow R_A + R_B = 1$$

$$\Rightarrow R_B = 1 - R_A$$

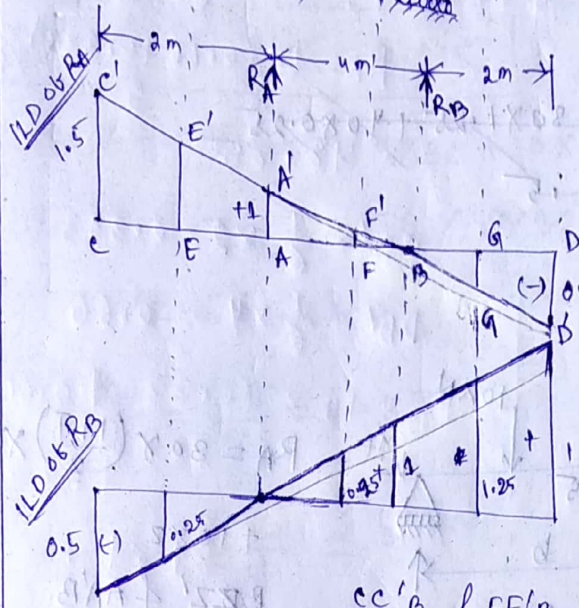
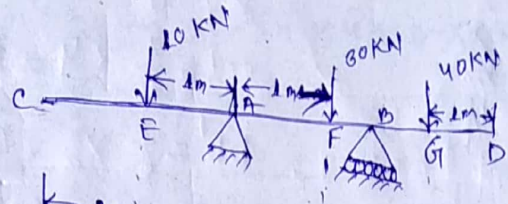
$$= 1 - \frac{3a - x}{2a}$$

$$= \frac{2a - 3a + x}{2a}$$

$$= \frac{x - a}{2a}$$

$R_A + R_B = 80$

Q



for span CA

$$R_A \times 4 = 10 \times (6-1)$$

$$R_A = \frac{50}{4} = 12.5$$

Load at RA, calculating by half of ILD.

$cc'B \Delta \& EE'B$

$$\frac{cc'}{Bc} = \frac{EE'}{BE}$$

$$\Rightarrow \frac{1.5}{6} = \frac{EE'}{5}$$

$$\Rightarrow EE' = 1.25$$

$cc'B \Delta \& FF'B$

$$\frac{cc'}{Bc} = \frac{FF'}{BF}$$

$$\Rightarrow \frac{1.5}{6} = \frac{FF'}{3}$$

$$\Rightarrow FF' = 0.75$$

$DD'B \Delta \& GG'B$

$$\frac{DD'}{BD} = \frac{GG'}{BG}$$

$$\Rightarrow \frac{0.5}{2} = \frac{GG'}{1}$$

$$\Rightarrow GG' = 0.25$$

$$R_A = 10 \times 1.25 + 30 \times 0.75 - 40 \times 0.25$$

$$= 12.5 + 22.5 - 10$$

$$= 25 \text{ KN}$$

$R_A + R_B = 80$

$\Rightarrow R_B = 80 - 25$

$R_B = 55 \text{ KN}$

$cc'A \Delta \& EE'A$

$$\frac{cc'}{Ac} = \frac{EE'}{AE}$$

$$= \frac{0.5}{2} = \frac{EE'}{1}$$

$$\Rightarrow EE' = 0.25$$

$ADD' \Delta \& AGG'$

$$\frac{DD'}{AD} = \frac{GG'}{AG}$$

$$\Rightarrow \frac{1.5}{6} = \frac{GG'}{5}$$

$$\Rightarrow GG' = 0.25$$

$ADD' \Delta \& AFF'$

$$\frac{DD'}{AD} = \frac{FF'}{AF}$$

$$\Rightarrow \frac{1.5}{6} = \frac{FF'}{1}$$

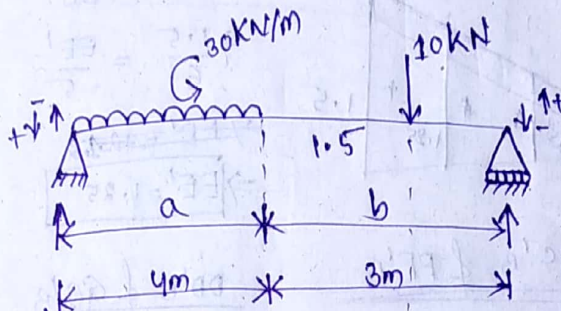
$$\Rightarrow FF' = 0.25$$

~~ADD' & ABB'~~

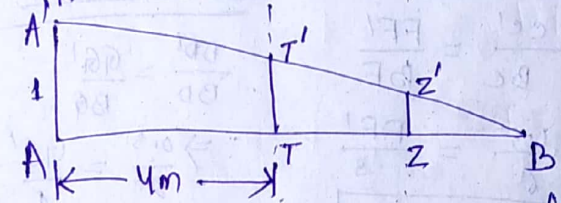
~~$\frac{DD'}{AD} = \frac{BB'}{AB}$
 $\Rightarrow \frac{1.5}{6} = \frac{BB'}{4}$
 $= BB' = 1$~~

~~$R_B = 10 \times (-0.25) - 30 \times 1.25 + 40 \times 0.25$
 $= -2.5 - 37.5 + 10$
 $= -50$~~

Q/



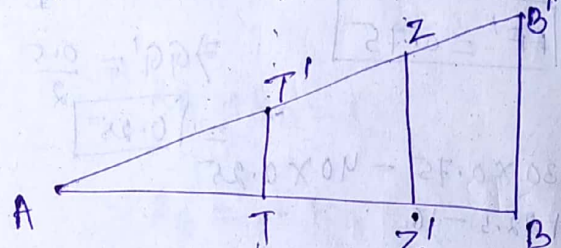
$R_A = 30 \times \left(\frac{1+7}{2}\right) \times 4$
 $+ 10 \times 2$
BBZ' & AA'B



$\frac{1}{L} = \frac{ZZ'}{1.5}$

$\Rightarrow \frac{1}{7} = \frac{ZZ'}{1.5}$

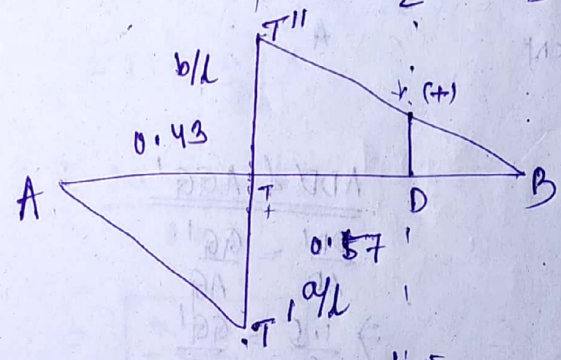
$\Rightarrow ZZ' = 0.214$



$\frac{1}{L} = \frac{TT'}{3}$

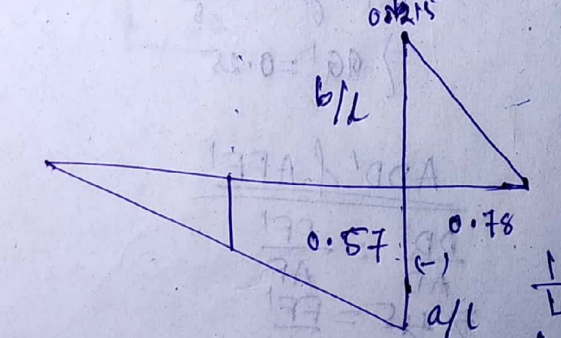
$\Rightarrow \frac{1}{7} = \frac{TT'}{3}$

$\Rightarrow TT' = 0.429$



$R_A = 30 \times \frac{1+0.429}{2} \times 4$

$+ 10 \times 0.214 = 87.88$



$\frac{1}{L} = \frac{ZZ'}{5.5}$

$\Rightarrow \frac{1}{7} = \frac{ZZ'}{5.5}$

$\Rightarrow ZZ' = 0.78$

$\frac{1}{L} = \frac{TT'}{4}$

$\frac{1}{7} = \frac{TT'}{4}$

$$TT' = 0.57$$

$$R_B = 30 \times \frac{1}{2} \times 0.57 \times 4 + 10 \times 0.78$$

$$= 42$$

$$DD' = \frac{0.43}{3} \times 1.5 = 0.215$$

$$SFC = -\frac{1}{2} \times 0.57 \times 4 \times 30 + 10 \times 0.215 = -32$$

$$SFD = \left(-\frac{1}{2} \times 0.56 \times 4 \times 30 \right) - 10 \times 0.78$$

$$= -41.4 \text{ kN/m}$$

$$\frac{b}{L} = \frac{1.5}{7} = 0.214$$

$$\frac{a}{L} = \frac{5.5}{7} = 0.78$$

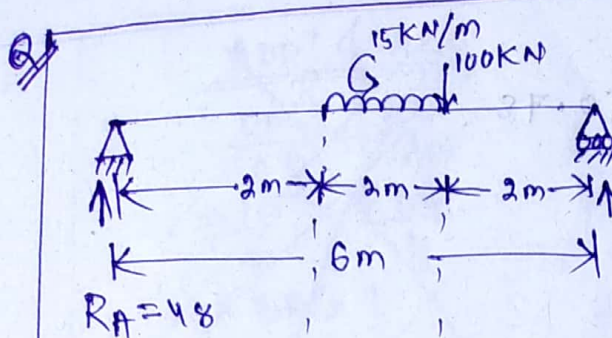
$$\frac{DD'}{AD} = \frac{cc'}{AC}$$

$$\Rightarrow \frac{0.78}{5.5} \times \frac{cc'}{4}$$

$$\Rightarrow cc' = 0.56$$

$$DD' = \frac{0.43}{3} \times 1.5 = 0.215$$

$$SFC = -\frac{1}{2} \times 4 \times 0.57 \times 30 + 10 \times 0.215 = -32$$



$$\sum V = 0$$

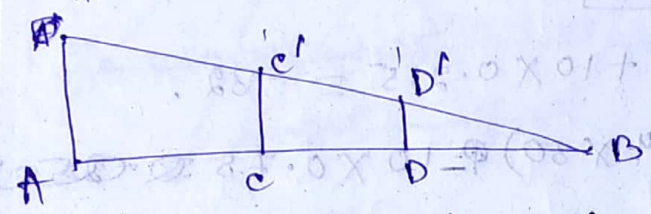
$$c c' = \frac{1}{6} \times 4 = 0.667$$

$$D D' = \frac{1}{6} \times 2 = 0.333$$

$$R_A = 48$$

$$R_B = 81.7$$

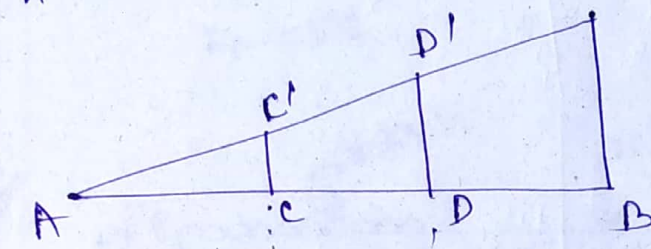
$$R_A = \frac{15(0.66 + 0.333)}{2} \times 2 + 100$$



$$= 48.85$$

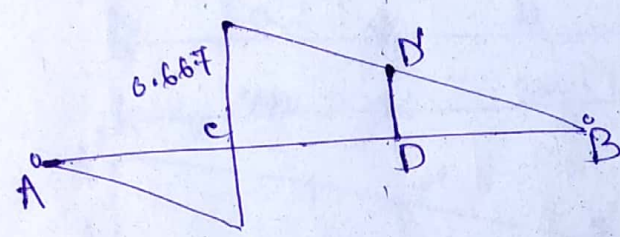
$$c c' = \frac{1}{6} \times 2 = 0.333$$

$$D D' = \frac{1}{6} \times 4 = 0.66$$



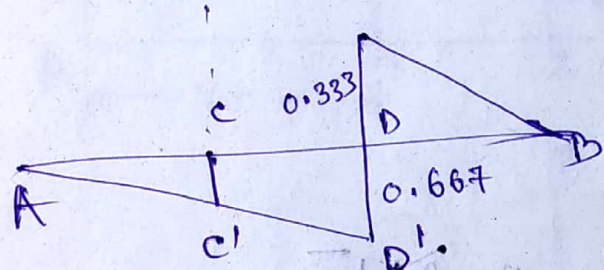
$$R_B = 15 \times \frac{(0.333 + 0.667)}{2} \times 2 + 100 \times 0.667$$

$$= 81.7$$



$$D D' = \frac{0.667}{4} \times 2 = 0.3335$$

$$SF = 100 \times 0.3335 + \frac{(0.667 + 0.3335)}{2} \times 2$$



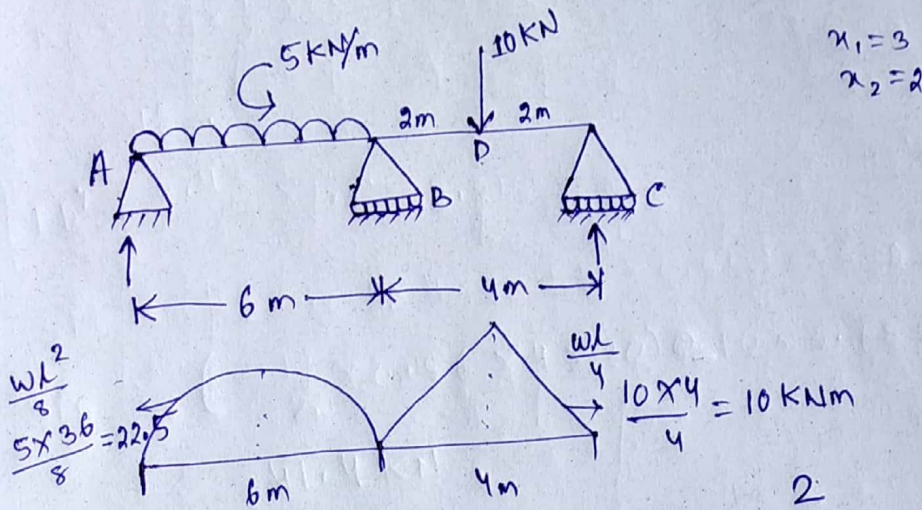
$$= 34.35$$

$$SF_c = \frac{0.667}{4} \times 2$$

$$= 0.3335$$

Formula:- $M_A l_1 + 2M_B (l_1 + l_2) + M_C l_2 + \frac{6A_1 x_1}{l_1} + \frac{6A_2 x_2}{l_2} = 0$

THREE MOMENT THEOREM



$$A_1 = \frac{2}{3} \times b \times h = \frac{2}{3} \times 6 \times 22.5 = 90 \text{ mm}^2$$

$$A_2 = \frac{1}{2} \times b \times h = \frac{1}{2} \times 4 \times 10 = 20 \text{ mm}^2$$

$$x_1 = 3$$

$$l_1 = 6$$

$$x_2 = 2$$

$$l_2 = 4$$

$$\begin{aligned} M_A &= 0 \\ M_C &= 0 \end{aligned}$$

$$M_A l_1 + 2M_B (l_1 + l_2) + M_C l_2 + \frac{6A_1 x_1}{l_1} + \frac{6A_2 x_2}{l_2} = 0$$

$$0 + 2M_B (6 + 4) + 0 + \frac{6 \times 90 \times 3}{6} + \frac{6 \times 20 \times 2}{4} = 0$$

$$\Rightarrow 2M_B \times 10 + 330 = 0$$

$$\Rightarrow M_B \times 20 = -330$$

$$\Rightarrow M_B = \frac{-330}{2} = -16.5$$